

(1)

DN PCSI / MP SI SLANT

Q1

$$I_2 r^2 \theta_{20}(r) = -kr (r \theta_{20}(r) - r \theta_{10}(r)) - kr (\theta_{20}(r) - \theta_{10}(r))$$

$$\frac{\theta_{20}(r)}{\theta_{10}(r)} = \frac{kr r + kr}{I_2 r^2 + kr (r + kr)}$$

$$= \frac{kr r + 1}{\frac{I_2}{kr} r^2 + r + 1}$$

$K = 1$        $\omega_0 = \sqrt{\frac{kr}{I_2}}$        $\frac{2\beta}{\omega_0} = \frac{kr}{kr}$

$$\Rightarrow \beta = \frac{kr}{2kr} \sqrt{\frac{kr}{I_2}} = \frac{kr}{2\sqrt{kr I_2}}$$

Q2)  $\beta = 0,7 \Rightarrow \beta = \frac{\sqrt{2}}{2} = \frac{kr}{2\sqrt{kr I_2}} \Rightarrow kr = \sqrt{2kr I_2}$

Q4

$$Q(r) = S r X(r) + \frac{V_0}{2B} r P(r)$$

$$P(r) = \frac{2B}{V_0 r} [Q(r) - S r X(r)]$$

$$P(r) = \underbrace{\left(\frac{2BS}{V_0}\right)}_{H_2} \left[ \underbrace{\left(\frac{1}{S r}\right)}_{H_1} Q(r) - X(r) \right]$$

Q3)  $k_{rev} = 16000$   
OK

Q5

$$I_3 r^2 \theta_{31}(r) + I_2 r^2 \theta_{21}(r) = d \times F(r)$$

②

$$\theta_{31}(T) = -\frac{I_2}{I_3} \theta_{21}(T) + \frac{d}{I_3 T^2} F(T)$$

$$H_4 = \frac{I_2}{I_3}$$

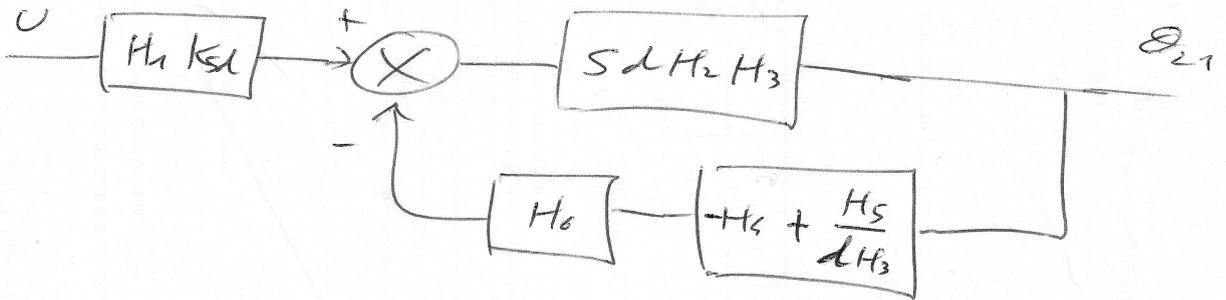
$$H_5 = \frac{d}{I_3 T^2}$$



Q6

$$H_6 = \frac{\lambda}{\theta_{31}} = \frac{\Delta \lambda}{\Delta \theta_{31}} = \frac{0,05}{0,1} = 0,5 \text{ m}$$

Q7



$$F(T) = \frac{H_1 K_{sd} \cdot S d H_2 H_3}{1 + S d H_2 H_3 H_6 \left( \frac{-d H_4 H_3 + H_5}{d H_3} \right)}$$

$$F(T) = \frac{\overset{AB}{S d H_2 H_3} \cdot H_1 K_{sd}}{1 + \underbrace{S H_2 H_6}_A \left[ H_5 - \underbrace{d H_3 H_4}_B \right]}$$

Q8

$$H(T) = \frac{K_c}{T(1+T) + K_c} = \frac{1}{\frac{T^2}{K_c} + \frac{T}{K_c} + 1} \quad | \quad K=1$$

$$\omega_0 = \sqrt{K_c} \quad ; \quad K=1$$

$$\frac{2\zeta}{\omega_0} = \frac{1}{K_c} \Rightarrow \zeta = \frac{1}{2\sqrt{K_c}}$$

$$\zeta = 1 \Rightarrow K_c = \frac{1}{4} = 0,25$$

Perf:  $\mu_{\text{cr}} K=1$

$$\omega_0 = 0,5 \quad t_{5\%} \omega_0 = 5$$

$$t_{5\%} = \frac{5}{0,5} = 10 \text{ s}$$