

(Dans les formules, u, v, f, g sont des fonctions réelles dérivables)

$$\bullet (u.v)' = u'.v + u.v'$$

$$\bullet \left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2}$$

$$\bullet \left(\frac{f}{g}\right)' = \frac{-g'}{g^2}$$

$$\bullet (\sqrt{x})' = \frac{1}{2\sqrt{x}} \quad \text{sur }]0, +\infty[\quad (= \mathbb{R}_+^*)$$

$$\bullet (\sqrt{u})' = \frac{u'}{2\sqrt{u}}$$

$$\bullet \left(\frac{1}{x}\right)' = \frac{-1}{x^2} \quad \text{sur } \mathbb{R}^*$$

$$\bullet \left(\frac{1}{u}\right)' = \frac{-u'}{u^2}$$

$$\bullet (\ln x)' = \frac{1}{x} \quad \text{sur }]0, +\infty[= \mathbb{R}_+^*$$

$$\bullet (\ln u)' = \frac{u'}{u}$$

$$\bullet (\exp x)' = \exp x \quad \text{sur } \mathbb{R}$$

$$\bullet (\exp u)' = \exp u \times u'$$

$$\bullet (x^n)' = n.x^{n-1}$$

$$\bullet (u^n)' = n.u^{n-1}.u'$$

$$\bullet \left(\frac{1}{x^n}\right)' = (x^{-n})' = (-n)x^{-n-1} = \boxed{\frac{-n}{x^{n+1}}}$$

$$\bullet (a^x)' = (e^{x \ln a})' = (\ln a).e^{x \ln a} = \boxed{(\ln a).a^x} \quad \text{sur } \mathbb{R} \text{ et } a > 0$$

$$\bullet (\sin x)' = \cos x \quad \text{sur } \mathbb{R}$$

$$\bullet (\cos x)' = -\sin x \quad \text{sur } \mathbb{R}$$

$$\bullet (\tan x)' = 1 + \tan^2 x = \frac{1}{\cos^2 x}$$

$$\bullet \varphi(x) = (f(g(x))) \quad \varphi'(x) = f'(g(x)) \times g'(x)$$

$$\bullet \varphi(x) = f(e^x) \quad \varphi'(x) = f'(e^x) e^x$$

$$\bullet \varphi(x) = f(\ln x) \quad \varphi'(x) = f'(\ln x) \frac{1}{x}$$

$$\bullet \varphi(x) = f(x^2) \quad \varphi'(x) = f'(x^2).2x$$